

SOLUTIONS MANUAL

THERMAL ENVIRONMENTAL ENGINEERING T H I R D E D I T I O N

**Thomas H. Kuehn
James W. Ramsey
James L. Threlkeld**

PRENTICE HALL , Upper Saddle River, NJ 07458

Acquisitions Editor: Laura Curless
Supplement Editor: Lauri S. Friedman
Special Projects Manager: Barbara A. Murray
Production Editor: Maria T. Molinari
Supplement Cover Manager: Paul Gourhan
Supplement Cover Designer: PM Workshop Inc.
Manufacturing Buyer: Dawn Murrin

© 2000 by Prentice Hall
Upper Saddle River, NJ 07458

All rights reserved. No part of this book may be
reproduced, in any form or by any means,
without permission in writing from the publisher.

Printed in the United States of America

10 9 8 7 6 5 4 3 2 1

ISBN 0-13-917238-6

Prentice-Hall International (UK) Limited, London
Prentice-Hall of Australia Pty. Limited, Sydney
Prentice-Hall Canada, Inc., Toronto
Prentice-Hall Hispanoamericana, S.A., Mexico
Prentice-Hall of India Private Limited, New Delhi
Pearson Education Asia Pte. Ltd., Singapore
Prentice-Hall of Japan, Inc., Tokyo
Editora Prentice-Hall do Brazil, Ltda., Rio de Janeiro

2.1

$$a) 28.75 \text{ in Hg} \left(\frac{1.450 \times 10^{-4} \text{ psia}}{2.961 \times 10^{-4} \text{ in Hg}} \right) = 14.08 \text{ psia}$$

$$b) 28.75 \text{ in Hg} \left(\frac{4.019 \times 10^{-3} \text{ in H}_2\text{O}}{2.961 \times 10^{-4} \text{ in Hg}} \right) = 390.2 \text{ in H}_2\text{O}$$

$$c) \frac{390.23 \text{ in H}_2\text{O}}{0.8} \left(\frac{1 \text{ m}}{39.37 \text{ in}} \right) = 12.39 \text{ m fluid}$$

$$d) 28.75 \text{ in Hg} \left(\frac{1 \text{ Pa}}{2.961 \times 10^{-4} \text{ in Hg}} \right) = 97.10 \text{ kPa}$$

2.2

a) Let x represent dry air and y represent water vapor. By Eqs. (2.18 and 2.19)

$$\frac{P_y}{P_x} = \frac{m_y}{m_x} \frac{R_y}{R_x}$$

$$m_y / m_x = 0.012$$

$$\frac{R_y}{R_x} = \frac{85.76 \text{ ft} \cdot \text{lb}_f / \text{lb}_m \cdot ^\circ\text{R}}{53.352 \text{ ft} \cdot \text{lb}_f / \text{lb}_m \cdot ^\circ\text{R}} = 1.607$$

$$P_x = P - P_y$$

Thus

$$P_y = \frac{P}{1 + \frac{m_x R_x}{m_y R_y}} = \frac{14.32 \text{ psia}}{1 + \frac{1}{(0.012)(1.607)}} = 0.27 \text{ psia}$$

$$b) \rho = \frac{m}{V} = \frac{m_x + m_y}{V} = \frac{m_x}{V} \left(1 + \frac{m_y}{m_x} \right)$$

$$\text{By Eq. (2.18), } \rho = \frac{P_x}{R_x T} \left(1 + \frac{m_y}{m_x} \right)$$

$$\rho = \frac{(14.32 - 0.27) \text{ lb}_f / \text{in}^2 (144 \text{ in}^2 / \text{ft}^2)}{\frac{53.352 \text{ ft} \cdot \text{lb}_f}{\text{lb}_m \cdot ^\circ\text{R}} (70^\circ\text{F} + 459.67^\circ\text{R})} \left(1 + 0.012 \right) = 0.0725 \frac{\text{lb}_m}{\text{ft}^3}$$

$$c) R = \frac{PV}{mT} = \frac{(14.32 \text{ lb}_f / \text{in}^2)(144 \text{ in}^2 / \text{ft}^2)}{(0.0725 \text{ lb}_m / \text{ft}^3)(70 + 459.67^\circ\text{R})} = 53.70 \frac{\text{ft} \cdot \text{lb}_f}{\text{lb}_m \cdot ^\circ\text{R}}$$

2.2 Cont'd

d) Based upon $m = m_x$, by Eq. (2.23)

$$c_p = c_{px} + \frac{m_y}{m_x} c_{py}$$

From Table A.5E, $c_{px} = c_{pa} = 0.2403 \text{ Btu/lb}_m^\circ\text{F}$ From Table A.6E, $c_{py} = c_{pv} = 0.450 \text{ Btu/lb}_m^\circ\text{F}$

$$c_p = 0.2403 + (0.012)0.450 = 0.246 \frac{\text{Btu}}{\text{lb}_m^\circ\text{F}}$$

2.3

Procedure follows that outlined in Prob. 2.2

$$a) m_y / m_x = 0.01 \text{ kg}_v / \text{kg}_a$$

$$P_y = \frac{95 \text{ kPa}}{1 + \frac{1}{(0.01)(1.607)}} = 1.50 \text{ kPa}$$

$$b) \rho = \frac{(95 - 0.01) \text{ kPa}}{\left(\frac{0.2870 \text{ kJ}}{\text{kg K}} \right) (20 + 273.15 \text{ K})} = 1.13 \text{ kg/m}^3$$

$$c) R = \frac{(95 \text{ kPa})}{(1.13 \text{ kg/m}^3)(20 + 273.15 \text{ K})} = 0.287 \text{ kJ/kg K}$$

$$d) \text{ From Table A.5 SI, } c_{p_x} = c_{p_a} = 1.006 \text{ kJ/kg}_a \text{ K}$$

$$\text{From Table A.6 SI, } c_{p_y} = c_{p_v} = 1.882 \text{ kJ/kg}_v \text{ K}$$

$$c_p = 1.006 + (0.01)(1.882) = 1.025 \text{ kJ/kg}_v \text{ K}$$

2.4

a) let ρ_1 be the correct density and ρ_2 the density computed using the perfect gas law

$$\text{By Eq. (2.24), } \frac{\rho_2}{\rho_1} = Z$$

By Fig. 2.1 at -20°F , 10 atm, $Z = 0.9892$

$$\text{Error} = (100) \frac{(\rho_1 - \rho_2)}{\rho_1} = 100(1 - 0.9892) = 1.08\%$$

$$\text{b) } P = 1 \text{ MPa} \left(\frac{10^3 \text{ kPa}}{1 \text{ MPa}} \right) \left(\frac{1 \text{ atm}}{101.325 \text{ kPa}} \right) = 9.87 \text{ atm}$$

By Fig. 2.1 at -30°C , 9.87 atm, $Z = 0.9895$

$$\text{Error} = 100(1 - 0.9895) = 1.05\%$$

2.5

By Table A.1E, $P = 0.95034 \text{ psia}$, $v = 349.98 \text{ ft}^3/\text{lb}_m$

$$R_v = 85.76 \text{ ft} \cdot \text{lb}_f / \text{lb}_m \cdot ^\circ\text{R}$$

Thus

$$Z = \frac{P_v}{RT} = \frac{(0.95034 \text{ lb}_f/\text{in}^2)(144 \text{ in}^2/\text{ft}^2)(349.98 \text{ ft}^3/\text{lb}_m)}{(85.76 \text{ ft} \cdot \text{lb}_f / \text{lb}_m \cdot ^\circ\text{R})(100 + 459.67 ^\circ\text{R})}$$

$$Z = 0.998$$

2.6

The energy balance on the radiator becomes

$$|\dot{Q}_{1-2}| = \dot{m}_{st} (h_1 - h_2)$$

$$\text{where } |\dot{Q}_{1-2}| = 5000 \text{ Btu/hr}$$

$$\text{at } \textcircled{1}, \text{ by Table A.1E, } h_f = 184.64, h_g = 1151.89 \frac{\text{Btu}}{\text{lbm}}$$

$$h_1 = h_f + x_1 (h_g - h_f) = 184.64 + 0.97(1151.89 - 184.64)$$

$$h_1 = 1122.87 \text{ Btu/lbm}$$

$$\text{at } \textcircled{2}, \text{ by Table A.1E, } h_2 = h_f(200^\circ\text{F}) = 168.34 \frac{\text{Btu}}{\text{lbm}}$$

Thus

$$\dot{m}_{st} = \frac{|\dot{Q}_{1-2}|}{h_1 - h_2} = \frac{5000 \text{ Btu/hr}}{(1122.87 - 168.34) \text{ Btu/lbm}}$$

$$\dot{m}_{st} = 5.24 \text{ lbm/hr}$$

2.7

The energy balance on the evaporator is

$$\dot{Q}_{1-2} = \dot{m}_{\text{ref}} (h_2 - h_1)$$

at ①, by Table A.2 SI, $h_f = 88.73$, $h_g = 1417.81 \frac{\text{kJ}}{\text{kg}}$

$$h_1 = 88.73 + 0.3(1417.81 - 88.73) = 487.45 \frac{\text{kJ}}{\text{kg}}$$

at ②, by Table A.2 SI, $h_2 = h_g = 1417.81 \frac{\text{kJ}}{\text{kg}}$

Thus

$$\dot{Q}_{1-2} = \frac{1 \text{ kg}}{\text{s}} \left(1417.81 - 487.45 \right) \frac{\text{kJ}}{\text{kg}} = 930.4 \text{ kW}$$

2.8

By Eq. (2.42)

$$\dot{I} = \dot{m}_{st} (s_2 - s_1) - \frac{\dot{Q}}{T_{air}}$$

at ①, by Table A.1E, $s_f = 0.31869$, $s_g = 1.7494 \frac{\text{Btu}}{\text{lbm}^\circ\text{R}}$

$$s_1 = s_f + x_1 (s_g - s_f) = 0.31869 + 0.97(1.7494 - 0.31869)$$

$$s_1 = 1.7065 \text{ Btu/lbm}^\circ\text{R}$$

at ②, by Table A.1E, $s_2 = s_f(200^\circ\text{F}) = 0.29430 \frac{\text{Btu}}{\text{lbm}^\circ\text{R}}$

Thus

$$\dot{I} = 5.24 \frac{\text{lbm}}{\text{hr}} (0.29430 - 1.7065) \frac{\text{Btu}}{\text{lbm}^\circ\text{R}} - \frac{(-5000) \text{ Btu/hr}}{(70 + 459.67^\circ\text{R})}$$

$$\dot{I} = 2.04 \frac{\text{Btu}}{\text{hr}^\circ\text{R}}$$

2.9

By Eq. (2.42)

$$\dot{I} = \dot{m}_{\text{ref}} (s_2 - s_1) - \frac{\dot{Q}_{1-2}}{T_{\text{air}}}$$

at ①, by Table A.2SI, $s_f = 0.3644$, $s_g = 5.6145 \frac{\text{kJ}}{\text{kg K}}$

$$s_1 = s_f + x_1 (s_g - s_f) = 0.3644 + 0.3(5.6145 - 0.3644)$$

$$s_1 = 1.9394 \text{ kJ/kg K}$$

at ②, by Table A.2SI, $s_2 = s_g(-20^\circ\text{C}) = 5.6145 \frac{\text{kJ}}{\text{kg K}}$

Thus

$$\dot{I} = \frac{1 \text{ kg}}{\text{s}} (5.6145 - 1.9394) \frac{\text{kJ}}{\text{kg K}} - \frac{930.4 \text{ kW}}{(-10 + 273.15 \text{ K})}$$

$$\dot{I} = 0.1395 \text{ kW/K}$$

2.10

By Eg. (2.86)

$$R_t = R_i + \left(\frac{l_1}{k_1} + \frac{l_2}{k_2} + \frac{l_3}{k_3} \right) + R_o$$

$$R_i = 1/h_i = 1/1.5 \text{ Btu/hr ft}^2\text{°F} = 0.667 \frac{\text{hr ft}^2\text{°F}}{\text{Btu}}$$

$$\frac{l_1}{k_1} = \frac{0.5 \text{ in}}{0.1 \text{ Btu/hr ft}^2\text{°F}} \left(\frac{\text{ft}}{12 \text{ in}} \right) = 0.417 \frac{\text{hr ft}^2\text{°F}}{\text{Btu}}$$

$$\frac{l_2}{k_2} = \frac{3.5 \text{ in}}{0.03 \text{ Btu/hr ft}^2\text{°F}} \left(\frac{\text{ft}}{12 \text{ in}} \right) = 9.722 \frac{\text{hr ft}^2\text{°F}}{\text{Btu}}$$

$$\frac{l_3}{k_3} = \frac{4.0 \text{ in}}{0.75 \text{ Btu/hr ft}^2\text{°F}} \left(\frac{\text{ft}}{12 \text{ in}} \right) = 0.444 \frac{\text{hr ft}^2\text{°F}}{\text{Btu}}$$

$$R_o = 1/h_o = 1/6 \text{ Btu/hr ft}^2\text{°F} = 0.167 \frac{\text{hr ft}^2\text{°F}}{\text{Btu}}$$

Thus

$$R_t = 0.667 + 0.417 + 9.722 + 0.444 + 0.167 = 11.417 \frac{\text{hr ft}^2\text{°F}}{\text{Btu}}$$

$$U = 1/R_t = 1/11.417 \text{ hr ft}^2\text{°F/Btu}$$

$$U = 0.0876 \text{ Btu/hr ft}^2\text{°F}$$

By Eg. (2.83), $Q/A = U(t_i - t_o)$

$$\frac{Q}{A} = \frac{0.0876 \text{ Btu}}{\text{hr ft}^2\text{°F}} (70 - 0)\text{°F} = 6.13 \frac{\text{Btu}}{\text{hr ft}^2}$$

2.11

We will use Eq. (2.52) to calculate h

$$\vec{V} = \frac{\dot{V}}{A} = \frac{2000 \text{ cm}^3/\text{s}}{\pi (3.0 \text{ cm})^2/4} = 2.83 \text{ m/s}$$

From Table A.6 SI

$$k = 0.6154 \text{ W/m}^\circ\text{C}$$

$$\mu = 797.7 \times 10^{-6} \text{ kg/ms}$$

$$\text{Pr} = 6.24$$

From Table A.1 SI

$$\nu_f = 0.001005 \text{ m}^2/\text{kg}$$

$$\text{Re}_D = \frac{(2.83 \text{ m/s})(0.03 \text{ m})}{(797.7 \times 10^{-6} \text{ kg/ms})(0.001005 \text{ m}^2/\text{kg})} = 1.059 \times 10^5$$

Flow is Turbulent so Eq. (2.52) is valid with the coefficients listed

$$h = \frac{k}{D} C \text{Re}_D^{0.8} \text{Pr}^{0.4}$$

$$h = \frac{0.6154 \text{ W/m}^\circ\text{C}}{0.03 \text{ m}} (0.023) (1.059 \times 10^5)^{0.8} (6.24)^{0.4}$$

$$h = 10,270 \text{ W/m}^2\text{C}$$

2.12

We will use Eq. (2.54) neglecting the viscosity ratio term to determine the heat transfer coefficient

$$Re_D = \bar{V} D / \nu = \rho \bar{V} D / \mu$$

From Table A.5E at the free stream temp.
of 70°F,

$$\rho = 0.07493 \text{ lb}_m / \text{ft}^3$$

$$\mu = 0.04400 \text{ lb}_m / \text{hr ft}$$

$$k = 0.01491 \text{ Btu} / \text{hr ft}^\circ\text{F}$$

$$Pr = 0.709$$

$$Re_D = \frac{(0.07493 \text{ lb}_m / \text{ft}^3)(10 \text{ ft/s})(5 \text{ in})}{(0.04400 \text{ lb}_m / \text{hr ft})(12 \text{ in} / \text{ft})} \left(\frac{3600 \text{ s}}{\text{hr}} \right) = 2.554 \times 10^4$$

$$h = \frac{k}{D} \left(0.4 Re_D^{0.5} + 0.06 Re_D^{2/3} \right) Pr^{0.4}$$

$$h = \frac{0.01491 \text{ Btu} / \text{hr ft}^\circ\text{F}}{5 \text{ in} (1 \text{ ft} / 12 \text{ in})} \left(0.4 (2.554 \times 10^4)^{0.5} + 0.06 (2.554 \times 10^4)^{2/3} \right) 0.709^{0.4}$$

$$h = 3.62 \text{ Btu} / \text{hr ft}^2 \cdot ^\circ\text{F}$$

$$\dot{Q} = h A (t_p - t_{air})$$

For 1 ft of pipe

$$\frac{\dot{Q}}{\text{ft}} = \frac{3.62 \text{ Btu}}{\text{hr ft}^2 \cdot ^\circ\text{F}} \left(\frac{\pi 5 \text{ in}}{12 \text{ in}} \right) \left(\frac{\text{ft}}{12 \text{ in}} \right) (150 - 70)^\circ\text{F} (1 \text{ ft})$$

$$\frac{\dot{Q}}{\text{ft}} = 379 \text{ Btu} / \text{hr}$$

2.13

The natural convection heat transfer coefficient will be determined from Eq. (2.57)

$$Ra_D = Gr_D Pr = \frac{g \beta D^3 \Delta t}{\nu^2} Pr = \frac{g \beta D^3 \Delta t}{(\mu/\rho)^2} Pr$$

From Table A.5E at the free stream temp. 70°F

$$\begin{aligned}\rho &= 0.07493 \text{ lb}_m / \text{ft}^3 \\ \mu &= 0.04400 \text{ lb}_m / \text{hr ft} \\ k &= 0.01491 \text{ Btu} / \text{hr ft}^\circ\text{F} \\ Pr &= 0.709\end{aligned}$$

$$\text{For gases, } \beta = \frac{1}{T} = 1 / (70 + 459.67^\circ\text{R}) = 1.888 \times 10^{-3} \text{ }^\circ\text{R}^{-1}$$

$$Ra_D = \frac{\left(\frac{32.174 \text{ ft}}{\text{s}^2} \right) \left(\frac{1.888 \times 10^{-3}}{^\circ\text{R}} \right) (5 \text{ in})^3 (150 - 70)^\circ\text{F} (0.709)}{\left(\frac{0.04400 \text{ lb}_m / \text{hr ft}}{0.07493 \text{ lb}_m / \text{ft}^3} \right)^2 \left(\frac{1728 \text{ in}^3}{\text{ft}^3} \right) \left(\frac{\text{hr}}{3600 \text{ s}} \right)^2}$$

$$Ra_D = 9.37 \times 10^6$$

By Eq. (2.57)

$$h_m = \frac{2 (0.01491 \text{ Btu} / \text{hr ft}^\circ\text{F}) / (5 \text{ in}) (1 \text{ ft} / 12 \text{ in})}{\ln \left[1 + \frac{2}{\left[\left(0.518 (9.37 \times 10^6) \right)^{1/4} \left[1 + \left(\frac{0.559}{0.709} \right)^{3/5} \right]^{-5/12} \right]^{15} + \left(0.1 (9.37 \times 10^6) \right)^{1/3} \right]^{15}} \right]^{1/15}}$$

$$h_m = 0.848 \text{ Btu} / \text{hr ft}^2 \text{ }^\circ\text{F}$$

$$\frac{\dot{Q}}{\text{ft}} = \frac{0.848 \text{ Btu}}{\text{hr ft}^\circ\text{F}} \left(\pi 5 \text{ in} \right) \left(1 \text{ ft} \right) \left(\frac{\text{ft}}{12 \text{ in}} \right) (150 - 70)^\circ\text{F} = 88.8 \text{ Btu} / \text{hr}$$

2.14

We will use Eq. (2.60) To determine the natural convection heat transfer coefficient in the window cavity with $L = 1\text{cm}$, $H = 1\text{m}$

$$Ra_L = \frac{g L^3 \Delta t Pr}{T (\mu/\rho)^2}$$

From Table A.5SI at 10°C

$$\rho = 1.248 \text{ kg/m}^3$$

$$\mu = 1.765 \times 10^{-5} \text{ kg/ms}$$

$$k = 0.02493 \text{ W/mK}$$

$$Pr = 0.712$$

$$Ra_L = \frac{(9.8 \text{ m/s}^2)(10^{-2} \text{ m})^3 (15^\circ\text{C})(0.712)}{(283.15 \text{ K}) \left(\frac{1.765 \times 10^{-5} \text{ kg/ms}}{1.248 \text{ kg/m}^3} \right)^2} = 1848$$

$$Nu_{L_{\text{conv}}} = \frac{1}{2} \left[\left(0.67 \left[1848 (0.01) \right]^{1/4} \left[1 + \left(\frac{0.559}{0.712} \right)^{3/5} \right]^{-5/12} \right)^{15} + \left(0.1 \left[1848 \right]^{1/3} \right)^{15} \right]^{1/15}$$

$$Nu_{L_{\text{conv}}} = 0.619$$

$$h_m = \frac{k}{L} \left[1 + \left(Nu_{L_{\text{conv}}} \right)^{15} \right]^{1/15}$$

$$= \frac{0.02493 \text{ W/mK}}{0.01 \text{ m}} \left[1 + (0.619)^{15} \right]^{1/15} = 2.493 \text{ W/m}^2 \text{K}$$

$$\dot{Q} = h_m A (t_h - t_c)$$

$$= \frac{2.493 \text{ W}}{\text{m}^2 \text{K}} (1 \text{ m}^2) (15^\circ\text{C}) = 37.4 \text{ W}$$

2.15

From Fig. 2.8 b

$$150 \text{ kPa} \rightarrow 10 \text{ kW/m}^2 \rightarrow h$$

$$h \approx 1500 \text{ W/m}^2\text{K}$$

$$q = h \Delta t$$

$$\Delta t = q/h = \frac{10 \text{ kW/m}^2}{1500 \text{ W/m}^2\text{K}} = 6.67 \text{ K}$$

From Table A.2 SI, the saturation temperature at 150 kPa is -25.23°C

Therefore the surface temperature becomes

$$t_{\text{surface}} = t_{\text{sat}} + 6.67^\circ\text{C}$$

$$= -25.23 + 6.67 = -18.56^\circ\text{C}$$

2.16

- a) We will use Eq. (2.61) to determine the heat transfer coefficient

From Table A.8E at 10°F

$$\begin{aligned}\mu_e &= 0.581 \text{ lb}_m / \text{ft hr} \\ k_e &= 0.0586 \text{ Btu/hr ft } ^\circ\text{F}\end{aligned}$$

From Table A.3E at 10°F

$$h_{fg} = h_g - h_f = 105.4 - 13.1 = 92.3 \text{ Btu/lb}_m$$

$$Re_e = \frac{1.0 \text{ lb}_m / \text{min} \left(\frac{12 \text{ in}}{\text{ft}} \right) (0.5 \text{ in})}{\frac{\pi (0.5 \text{ in})^2}{4} (0.581 \text{ lb}_m / \text{ft hr}) \left(\frac{60 \text{ min}}{\text{hr}} \right)} = 3156$$

$$\text{Let } L = 10 \text{ ft}$$

$$K = \frac{778 \text{ ft lb}_m}{\text{Btu}} \frac{0.8 (92.3 \text{ Btu/lb}_m)}{10 \text{ ft}} = 5745$$

$$h_m = \frac{(0.0586 \text{ Btu/hr ft } ^\circ\text{F}) 0.0082 (3156^2 (5745))^{0.4}}{(0.5 \text{ in}) (\text{ft}/12 \text{ in})}$$

$$h_m = 231 \text{ Btu/hr ft } ^2\text{ } ^\circ\text{F}$$

(different choice of L will affect values for K and h_m)

- b) The length necessary will depend on the temperature difference maintained between the tube and the fluid

For our choice of 10 ft in part a,

$$\dot{Q} = h_m A \Delta t = \dot{m} \Delta x h_{fg}$$

$$\text{or } \Delta t = \dot{m} \Delta x h_{fg} / (h_m A)$$

$$\Delta t = \frac{(10 \text{ lb}_m / \text{min}) 0.8 (92.3 \text{ Btu} / \text{lb}_m) \left(\frac{60 \text{ min}}{\text{hr}} \right) \left(\frac{12 \text{ in}}{\text{ft}} \right)}{\left(\frac{231 \text{ Btu}}{\text{hr ft}^2 \text{ } ^\circ\text{F}} \right) (\pi 0.5 \text{ in } 10 \text{ ft})}$$

$$\Delta t = 15 ^\circ\text{F}$$

if the temperature difference is one-half this value, the necessary length would be doubled to 20 ft

2.17

We will use Eq. (2.63)

From Table A.8E at 100°F

$$\begin{aligned}c_{pe} &= 0.3162 \text{ Btu/lbm}^\circ\text{F} \\ \mu_e &= 0.338 \text{ lbm/ft hr} \\ k_e &= 0.0466 \text{ Btu/hr ft}^\circ\text{F} \\ Pr_e &= 2.29\end{aligned}$$

From Table A.3E at 100°F

$$\begin{aligned}\rho_e &= 71.24 \text{ lbm/ft}^3 \\ \rho_w &= 3.89 \text{ lbm/ft}^3 \\ h_{fg} &= 72.80 \text{ Btu/lbm}\end{aligned}$$

$$Re_c = \frac{(1.0 \text{ lbm/min})(0.5 \text{ in})}{\pi (0.5 \text{ in})^2 \frac{0.338 \text{ lbm}}{\text{hr ft}}} \left(\frac{71.24}{3.89} \right)^{0.5} \left(\frac{12 \text{ in}}{\text{ft}} \right) \left(\frac{60 \text{ min}}{\text{hr}} \right) = 23,214$$

$$M = \frac{72.80 \text{ Btu/lbm}}{0.3162 \text{ Btu/lbm}^\circ\text{F} (8^\circ\text{F})} = 28.78$$

$$Nu_e = 0.1 (2.29)^{1/3} (28.78)^{1/6} (23,214)^{2/3} = 188$$

$$h = \frac{188 (0.0466 \text{ Btu/hr ft}^\circ\text{F})}{0.5 \text{ in}} \left(\frac{12 \text{ in}}{\text{ft}} \right) = 210 \frac{\text{Btu}}{\text{hr ft}^2^\circ\text{F}}$$

2.18

Using Eq. (2.74) with $\epsilon_1 = 1$, $\epsilon_2 = 1$, and $F_{1-2} = 1.0$

$$\frac{\dot{Q}_{1-2}}{A_1} = \sigma (T_1^4 - T_2^4)$$

$$= 0.1713 \frac{\text{Btu}}{\text{hr ft}^2 \text{ } ^\circ\text{R}^4} \left[(10 + 459.67)^4 - (-40 + 459.67)^4 \right] \text{ } ^\circ\text{R}^4$$

$$\frac{\dot{Q}_{1-2}}{A_1} = 30.22 \frac{\text{Btu}}{\text{hr ft}^2}$$

2.19

We will use the following equation assuming the surroundings behave as a black body at 70°F

$$\dot{Q}_{1-2} = \epsilon_1 A_1 \sigma (T_1^4 - T_2^4)$$

for a length of 1 ft

$$\frac{\dot{Q}_{1-2}}{\text{ft}} = 0.85 \frac{\pi \sin(1 \text{ ft})}{(12 \text{ in} / \text{ft})} 0.1713 \times 10^{-8} \frac{\text{Btu}}{\text{hr ft}^2 \cdot \text{R}^4} (609.67^4 - 529.67^4) \text{R}$$

$$\frac{\dot{Q}_{1-2}}{\text{ft}} = \frac{113 \text{ Btu}}{\text{hr}}$$

2.20

We will use Eq. (2.74) with $F_{1-2} = 1.0$ and $A_1 / A_2 = 1.0$

$$\begin{aligned}\dot{Q}_{1-2} &= \frac{A_1 \sigma (T_1^4 - T_2^4)}{\frac{1}{\epsilon_1} + \frac{1}{\epsilon_2} - 1} \\ &= \frac{1 \text{ m}^2 (5.670 \times 10^{-8} \text{ W/m}^2 \text{ K}^4) (288.15 \text{ K}^4 - 273.15 \text{ K}^4)}{\frac{1}{0.9} + \frac{1}{0.9} - 1}\end{aligned}$$

$$\dot{Q}_{1-2} = 61.6 \text{ W}$$

2.21

Let the radiative heat transfer be written as

$$\dot{Q}_r = h_r A (t_1 - t_2)$$

$$h_r = \frac{\dot{Q}_r}{A (t_1 - t_2)}$$

$$= \frac{113 \text{ Btu/hr} (12 \text{ in/ft})}{\pi 5 \text{ in} (1 \text{ ft}) (150 - 70)^\circ\text{F}} = \frac{1.079 \text{ Btu}}{\text{hr ft}^2^\circ\text{F}}$$

The combined convective / radiative heat transfer coefficient becomes

$$h = h_c + h_r$$

$$= 0.848 + 1.079 = \frac{1.927 \text{ Btu}}{\text{hr ft}^2^\circ\text{F}}$$

2.22

Let the radiative heat transfer coefficient be written as

$$h_r = \frac{\dot{Q}_r}{A(t_1 - t_2)}$$
$$= \frac{61.6 \text{ W}}{1 \text{ m}^2 (15 - 0)^\circ\text{C}} = \frac{4.11 \text{ W}}{\text{m}^2^\circ\text{C}}$$

The combined convective/radiative heat transfer coefficient becomes

$$h = h_c + h_r$$
$$= 2.493 + 4.11 = \frac{6.60 \text{ W}}{\text{m}^2^\circ\text{C}}$$